# Similarity and Transformations

## This booklet belongs to:

LESSON #			Overstiens that T
LE330N #	DATE	QUESTIONS FROM	Questions that I
		NOTES	find difficult
1.		Pg.	
2.		Pg.	
3.		Pg.	
4.		Pg.	
5.		Pg.	
6.		Pg.	
7.		Pg.	
8.		Pg.	
9.		Pg.	
10.		Pg.	
11.		REVIEW	
12.		TEST	

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Your teacher has important instructions for you to write down below.

Unless otherwise stated, round your final answer to one decimal place.

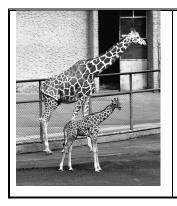
# Similarity and Transformations

IRP	#	Daily Topic	Key Ideas
C3 Demonstrate an understanding of	1.	Scale Drawings (pg. 4-8) Determine the scale factor for a given diagram drawn to scale.	
similarity of polygons. [C, CN, PS, R, V] C4 Draw and interpret scale diagrams of 2-D shapes.	2.	<ul> <li>Scale Drawings Con't (pg. 8-11)</li> <li>Determine if a given diagram is proportional to the original 2-D shape and, if it is, state the scale factor.</li> <li>Draw a diagram to scale that represents an enlargement or reduction of a given 2-D shape</li> </ul>	
[CN, R, T, V]	3.	Applying scale drawings (pg. 12-16)	
	4.	Extra Day for Scale drawings	
	5.	<ul> <li>Similar polygons (Pg. 17-22)</li> <li>Determine if the polygons in a given pre-sorted set are similar and explain the reasoning.</li> <li>Draw a polygon similar to a given polygon and explain why the two are similar.</li> </ul>	
	6.	<ul> <li>Similar Triangles (Pg. 23-28)</li> <li>Solve a given problem that involves a scale diagram by applying the properties of similar triangles</li> <li>Identify an example in print and electronic media (e.g., newspapers, the Internet) of a scale diagram and interpret the scale factor.</li> </ul>	
C5 Demonstrate an understanding of line and rotation symmetry. [C, CN, PS, V]	7.	<ul> <li>Line Symmetry (Pg. 29-33)</li> <li>Classify a given set of 2-D shapes or designs according to the number of lines of symmetry</li> <li>Complete a 2-D shape or design given one half of the shape or design and a line of symmetry</li> <li>Identify the type of symmetry that arises from a given transformation on the Cartesian plane.</li> </ul>	
	8.	<ul> <li>Rotational Symmetry (Pg. 34-37)</li> <li>Determine if a given 2-D shape or design has rotation symmetry about the point at the centre of the shape or design and, if it does, state the order and angle of rotation.</li> <li>Rotate a given 2-D shape about a vertex and draw the resulting image.</li> </ul>	
	9.	<ul> <li>Rotational Symmetry con't (Pg. 38-42)</li> <li>Complete, concretely or pictorially, a given transformation of a 2-D shape on a Cartesian plane, record the coordinates, and describe the type of symmetry that results.</li> <li>Determine whether or not two given 2-D shapes on the Cartesian plane are related by either rotation or line symmetry.</li> <li>Draw, on a Cartesian plane, the translation image of a given shape using a given translation rule, such as R2, U3, label each vertex and its corresponding ordered pair, and describe why the translation does not result in line or rotation symmetry.</li> <li>Create or provide a piece of artwork that demonstrates line and rotation symmetry, and identify the line(s) of symmetry and the order and angle of rotation.</li> </ul>	
	10.	<ul> <li>Chapter Review and Practice Test</li> <li>Help students develop sound study habits.</li> <li>Many students will graduate high school saying they do not know how to study for math tests.</li> </ul>	
	11.	• Go over Practice Test	
	12.	Unit Evaluation	

Key Terms

		<b>F</b>
	Definition	Example
Angle of rotation	The smallest angle needed for a shape to rotate	
symmetry	to match itself.	
Cartesian plane	A two dimensional surface made up of	
	coordinates. The vertical axis is called the y- axis	
	and the horizontal axis is called the x-axis.	
Corresponding	Angles that match in similar polygons.	
angles		
Corresponding	Side lengths that match in similar polygons.	
lengths	Side lengths that match in similar polygons.	
longino		
Corresponding	Sides that match in similar polygons.	
sides		
Order of rotation	The number of times a shape matches itself	
	during a rotation of 360°.	
	<u> </u>	
Polygon	A closed shape. i.e. triangle, circle	
Proportion	Having the same ratio.	
Detetionel	The property of a abane where it are retated and	
Rotational	The property of a shape where it can rotate less	
symmetry	than 360° and match itself.	
Scale drawing	A drawing that is an enlargement or a reduction	
_	of another drawing.	
Scale factor	The common number that is used to multiply or	
	divide side lengths to create a similar polygon.	
Similar Polygons	Two polygons with the same shape and	
	Equal corresponding angles	
	Equal ratio of pairs of corresponding sides	

## Scale Drawings



How many times larger does the taller giraffe look compared to the smaller one?

The answer to question above is called the scale factor.

- If an object is 5 times bigger then the scale factor is 5.
- If an object is half as big then the scale factor is 0.5.
- If a scale drawing is 4cm long and the actual length is 400cm then the scale factor would be 1/100.

## Challenge #1:

<ol> <li>Determine the scale factor for each scale drawing. The original image is on the left.</li> </ol>	<ol> <li>Determine the scale factor for each scale drawing. The original image is on the left.</li> </ol>	3. Draw the figure below with a scale factor of 2. Is this an enlargement or a reduction?					

6.

### Challenge #2:

5. A grey nurse shark is 358cm long. National geographic has a

photograph of the same shark and it measures 5.2cm long. How many times bigger is the real shark compared to the picture? James is creating replica of a Bell 412 rescue helicopter from a photograph with a width of 2.8cm and a total length of 17cm. Determine the new dimensions if the scale factor is 8.

### Definitions

Proportionate: Having a constant ratio to another quantity.

#### Scale Drawing:

- A drawing that is proportionate to another drawing.
- This means that corresponding pairs of side lengths are equal.

#### Scale Factor:

• The common number that is used to multiply or divide side lengths to create a similar polygon. Reduction:

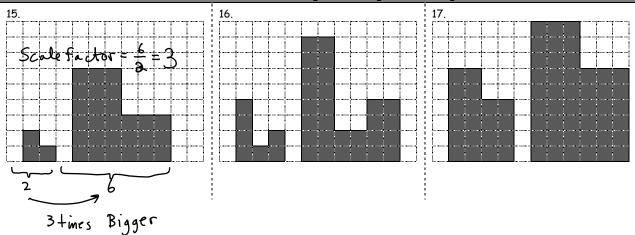
- Creates a smaller image.
- The scale factor for reductions is between 0 and 1.

Enlargement:

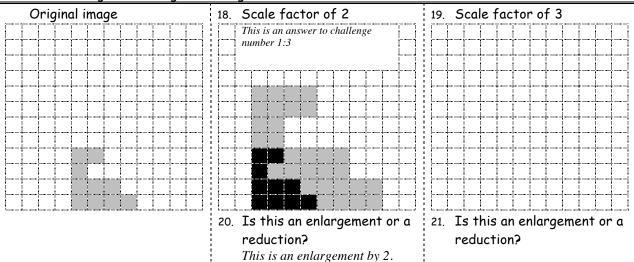
- Creates a larger image.
- The scale factor for enlargements is greater than 1.

Write each scale factor as a decimal and state whether it will create an enlargement or a reduction. (Round your answer to 2 decimal places)

7.	200 1000	8. <u>350</u> 50	9. <u>140</u> 200	10. $\frac{20}{1000}$
11.	25	12. <mark>80</mark>	13. <u>900</u>	14. <u>500</u>
	125	4000	3000	80

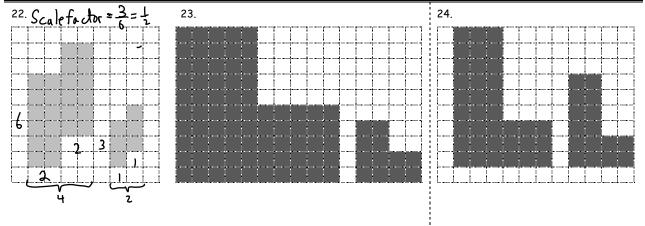


#### Determine the scale factor for each scale drawing. The original drawing is on the left.



#### Redraw the original drawing with the given scale factors:

Determine the scale factor for each scale drawing. The original drawing is on the left.



Determine the scale factor or the actual size. Round your answer to 2 decimal places.

25. A grey nurse shark is 358cm long. National geographic has a photograph of the same shark and in the picture the shark measures 5.2cm. Determine the scale factor. Photo = 5.2 cmReallift = 358S cole factor = 0.01

A drawing of a bedbug is
 2.2cm long. The actual size is 0.95cm. Determine the scale factor.



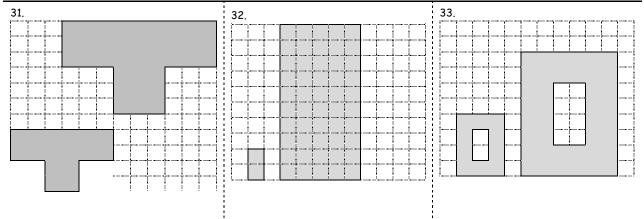
27. This is a picture of a prehistoric scorpion. The drawing measures at 2.5 centimeters long. If the scale factor is 1/110, determine the actual length of a prehistoric scorpion.



Determine the scale drawings dimensions. (Round your answer to 2 decimals)

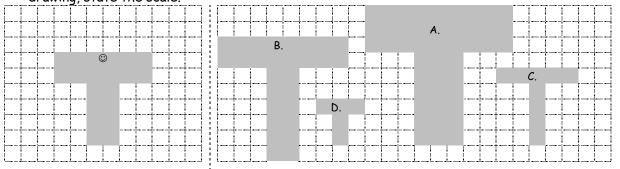
28. James is creating replica of	29. Vince is creating a replica	30. In the photo the wingspan
a Bell 412 rescue helicopter	of an AW 139 rescue	of Boeing 777 is 6.1cm long
from a photograph with a	helicopter from a	and the height of the plane
width of 2.8cm and a total	photograph with a blade	is 1.9cm tall. Randal plans
length of 17cm. Determine	diameter of 13.8cm. How	to make a replica using a
the new dimensions if the	long will the replica blade	scale factor of 3.8.
scale factor is 8.	length be <u>if</u> the scale	Determine the new
Photo -> Replica	factor is D	dimensions.
2.8cm × 8 = 22.4cm	factor is ?	
17cm × 8= 136cm		
The new dimensions are		
22.4cm Wido &		
136 cm long.		
Ũ		

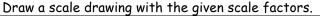
#### Determine the scale factor for each scale drawing. The original drawing is on the left.

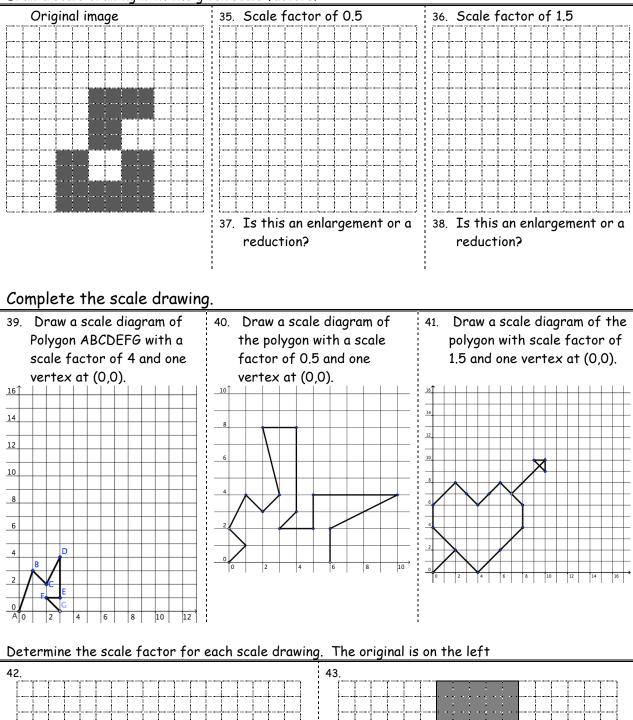


#### Proportionate drawings

34. Which of the shapes below are proportionate to the shape marked ©? If the figure is a scale drawing, state the scale.

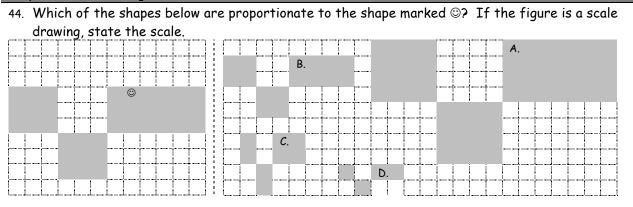




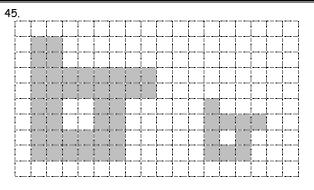


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Proportionate drawings.

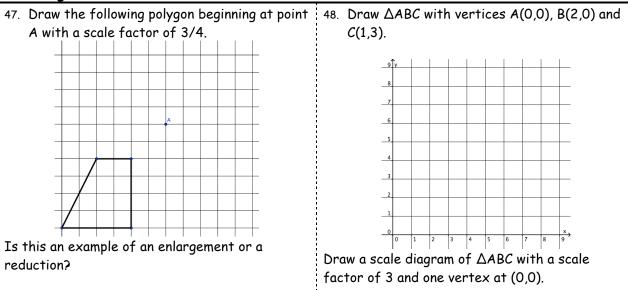


#### Determine the scale factor for each scale drawing. The original is on the left

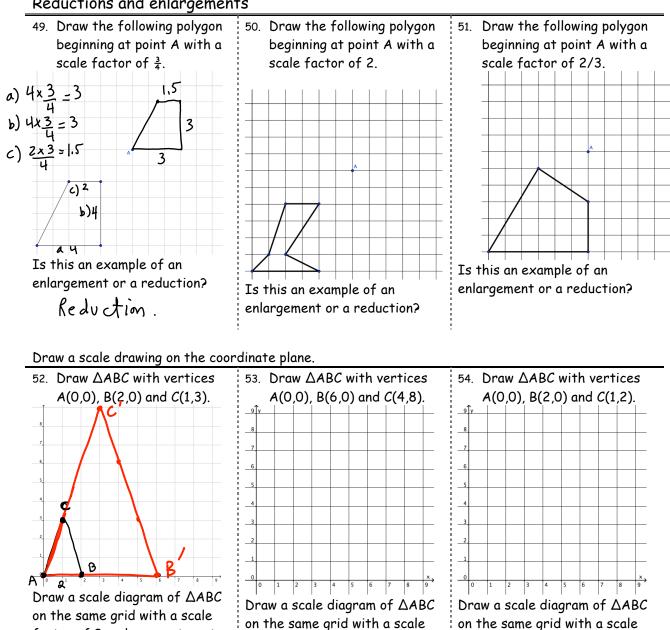


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## Challenge #3:

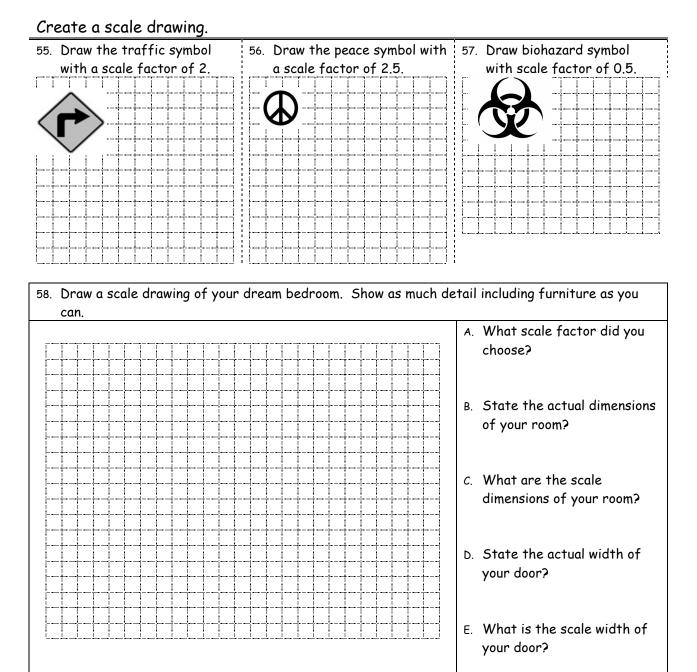


**Reductions and enlargements** 



factor of 3 and one vertex at factor of 0.5 and one vertex at (0,0).  $AB = 2 \times 3 = 6$   $Point = (1,3) \Rightarrow (3,9)$ (0,0).

on the same grid with a scale factor of 2.5 and one vertex at (0,0).



## Applications of Scale Drawings

#### Notes:

	Millimeters	Centimeters	Meters	Kilometers
59.	1200mm	Α.	В.	С.
60.	Α.	20000cm	В.	С.
61.	Α.	B.	50m	С.
62.	A.	B.	С.	7km

#### Challenge #4: Fill out the table.

\*1 km = 1000m, 1 m=100cm and 1cm=10mm.

#### Challenge #5:

63. A whale shark measures 30m long. Determine the scale factor if it measures 8cm in the photograph.



64. This is a dust mite and it eats your dead skin. It is 27mm in this picture. Its actual length is 0.045mm. Determine the scale factor.

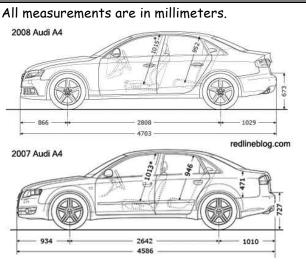
<u>Conversions</u>.

65. Convert 0.56km to cm.	66. Convert 7888m to	67. Convert 11.7km to meters.
Possible solution:	kilometers.	
0.56km→560m→56000cm		
(1km=1×1000m=1×1000×100cm)		
68. Convert 44cm to	69. Convert 3720cm to meters.	70. Convert 22cm to
millimeters.		kilometers.

Determine the scale factor. Round your answer to four decimals.

Determine the scale factor. Rou	ind your answer to four decimals.	
<ul> <li>71. A whale shark measures 30m long. Determine the scale factor if it measures 8cm in the photograph.</li> <li>Possible Solution: Actual 30m→3000cm Photograph→8cm</li> <li>=0.0027</li> </ul>	72. The tallest coast Douglas fir measures 94m. Wonita drew a picture of it that measures 11cm tall. Determine the scale factor.	<ul> <li>73. The distance between</li> <li>Victoria and Comox on a map is 23.2cm. The actual distance is between the two cities is 180 kilometers.</li> <li>Determine the scale factor to 8 decimals.</li> </ul>
<ul> <li>74. The tallest redwood tree in world measures 5.4 cm in a photograph. Its actual height is 115m tall. Determine the scale factor.</li> </ul>	<ul> <li>75. A drawing of an Asian Long Horned Beetle is 2.4 cm long. The actual length is 32 mm. Determine the scale factor.</li> </ul>	76. The greatest gap between rims in the Grand Canyon on a map is 2.9 cm. Determine the actual gap in km, if the scale factor is 1/1000000.
<ul> <li>77. This is a dust mite and it eats your dead skin. It is 27mm in this picture. Its actual length is 0.045mm. Determine the scale factor to 1 decimal.</li> <li>Possible Solution: Actual → 0.0045mm Picture → 27mm</li> </ul>	78. This is a picture of a type of mold that can cause hazards for many people. It measures 1.7 cm in this picture but actually measures. 0.0003cm. Determine the scale factor to 1 decimal.	79. The smallest gap between rims in the Grand Canyon 549m. Determine the length of this gap on a map in cm if the scale factor is 1/90000. Round your answer to 2 decimals.

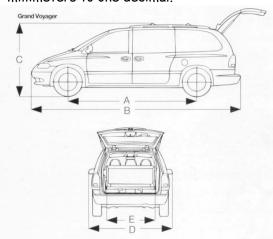
## Scale drawing problems.



80. Jason decides to make a replica of a 2007 Audi A4 and a 2008 Audi A4. Each vehicle will have a scale factor of 1/70. How much longer will the 2008 A4 be than the 2007 A4? Round your answer to one tenth of a mm.

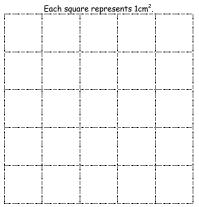
## Challenge #3:

 Sarender plans to make a replica of a Grand Voyager. She wants it to be one meter long. Determine the height and width in millimeters to one decimal.



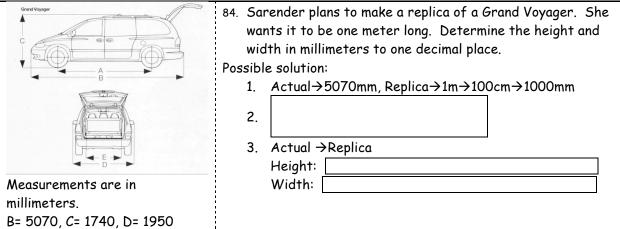
Measurements are in millimeters. B=5070, C=1740, D=1950

82. The dimensions for an indoor volleyball court are 18m by 9m. Draw a scale drawing with a scale factor of 1/500.



83. The attack line is 3m from the net. Back row players must jump behind this line to spike the ball. How far is this line from the net in the scale drawing?

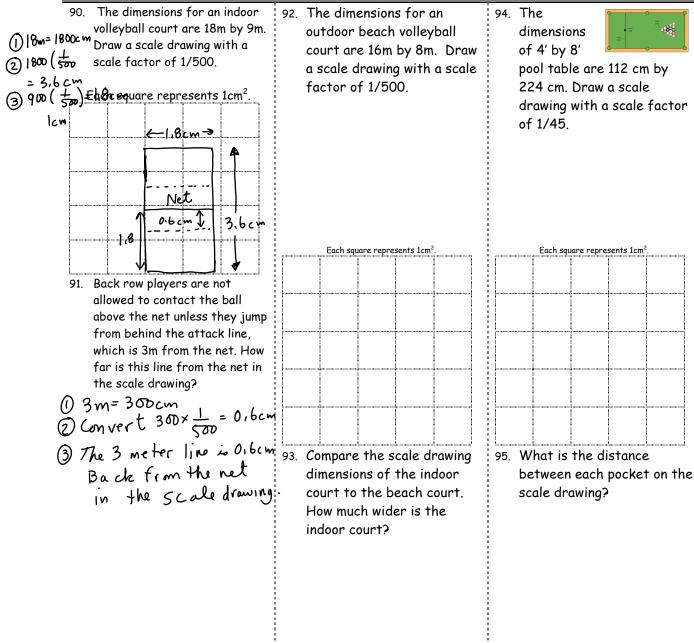
### Scale drawing problems.



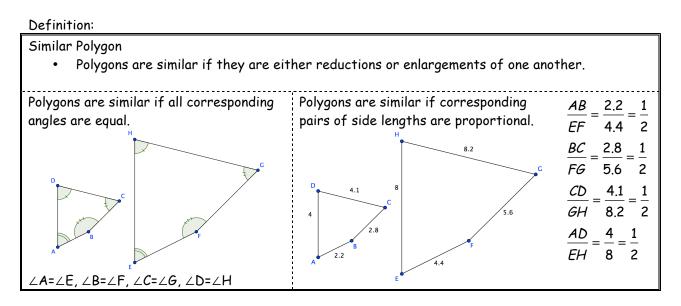
#### Building a model car. (Round your answer to the nearest hundredth of a cm.)

All measurements are in millimeters.	Volksv chargu replica vehicl room. to be	ust got a job at vagen and is in e of creating a models of the es for the show The replica needs 20cm long. mine the scale	86.	If the replica must be 20cm long, how tall will it be if the replica is perfectly proportional?
87. John is creating a small- motorized version for the owner's child. The vehicle will be 100 cm wide from the outer edge of each mirror. Determine the scale factor.	from	e width is 100cm nirror to mirror, all will the vehicle	89.	If the width is 100cm from mirror to mirror, how far apart will the center of the wheels be?

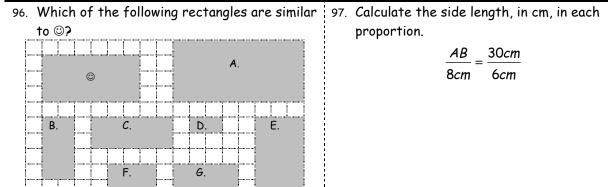




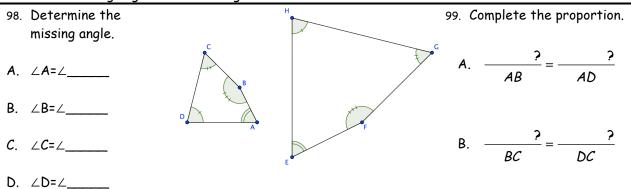
## Similarity

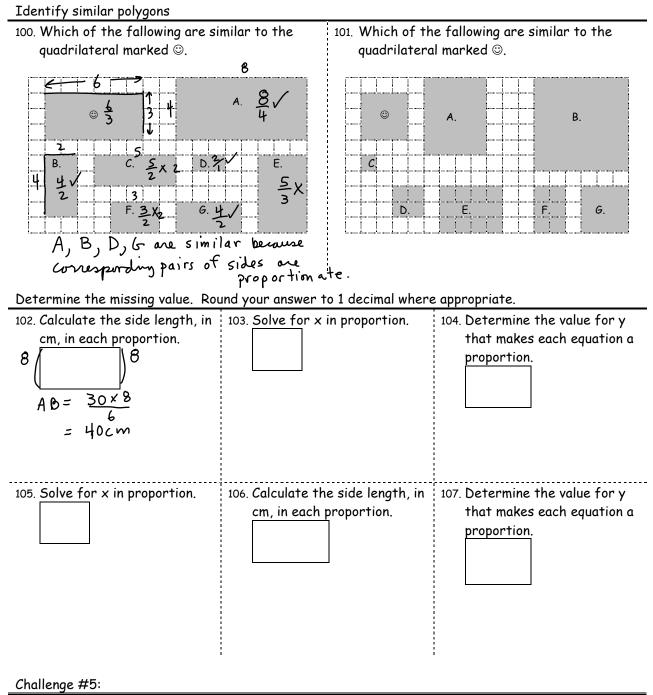


Challenge #4:



#### Fill in the missing angles and side lengths.





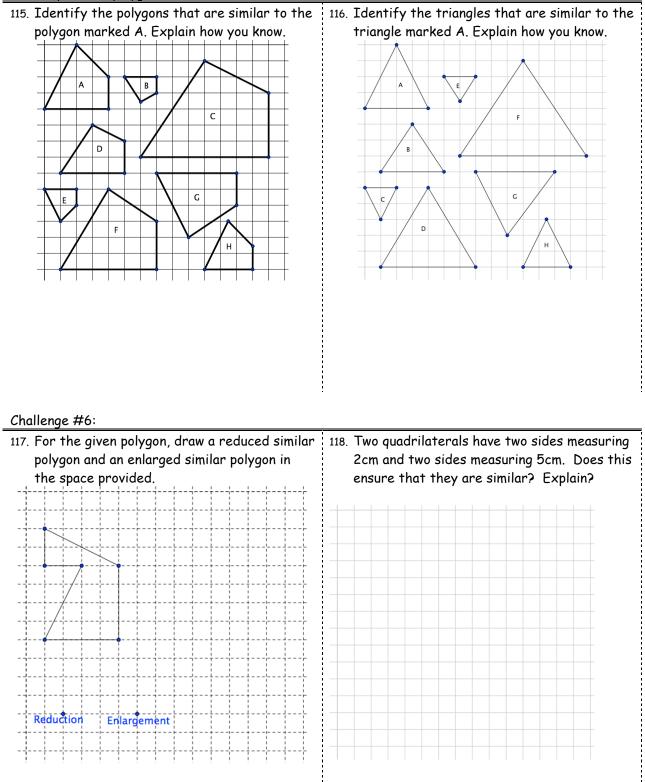
108. Draw two rectangles with following dimensions:
45.8m by 24.6m
22.9m by 12.8m
Are the two rectangles similar? Explain

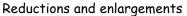
Are the two rectangles similar? Explain how you know.

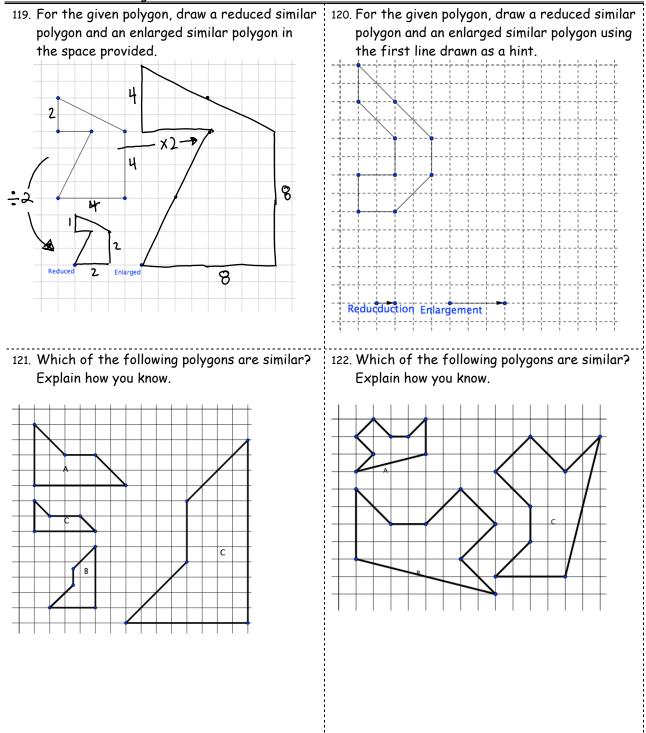
Sketch each pai	ir of poly	gons and de	termine if th	ey are similar	or not? Ex	plain how y	you know.
-----------------	------------	-------------	---------------	----------------	------------	-------------	-----------

Sketch each pair of polygons and determine if they are similar of not? Explain now you know.				
109. Draw two rectangles with	110. Draw two rectangles with	111. Draw two right triangles		
following dimensions:	following dimensions:	with following dimensions:		
<ul> <li>45.8m by 24.6m</li> </ul>	<ul> <li>15.55m by 13.24m</li> </ul>	<ul> <li>25.56m by 17.86m</li> </ul>		
<ul> <li>22.9m by 12.8m</li> </ul>	<ul> <li>62.2m by 52.96m</li> </ul>	• 6.39m by 4.565m		
$45.8$ $22.9$ $45.8$ $22.9$ $12.8$ Check $\frac{45.8}{24.6} = 1.86179$ $\frac{22.9}{12.8} = 1.78906$ Since the rations of corresponding airs of sides are not equal, the two rectangles are not sime.	۰. م			
112. Draw two right triangles	113. Draw two equilateral	114. Draw two isosceles		
with following dimensions:	triangles. Do they have to	triangles. Do they have to		
<ul> <li>20.91m by 17.72m</li> <li>8.30m by 5.56m</li> </ul>	be similar? Explain.	be similar? Explain.		
• 8.39m by 5.56m				

#### Identify similar polygons.

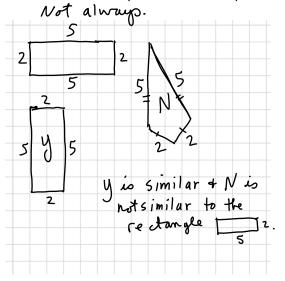




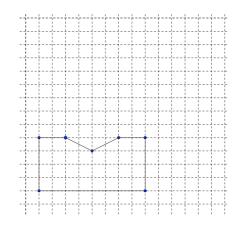


Think about it!

123. Two quadrilaterals have two sides measuring 2cm and two sides measuring 5cm. Does this ensure that they are similar? Explain.



124. Draw a polygon by reducing each side length by half. Is it possible for the polygon not to be similar? Explain.



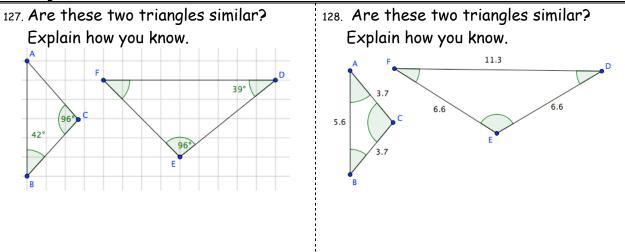
Round your answer to three decimals.

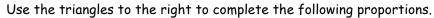
- 125. An Imax screen is 8 stories tall which makes it 21.5 m wide and 15.6 meters tall. Jimmy just bought a 46-inch TV, which is 1.17m wide. How tall will he want to make the vertical height on his TV to match Imax proportions?
- 126. Jimmy made a small miscalculation and realized that when the movie did not fit on the screen. He forgot that TVs are measured by their diagonal length not their horizontal. So 1.17m is actually the diagonal length not the horizontal length. Determine the actual width and height that he should set his TV to watch Imax movies.

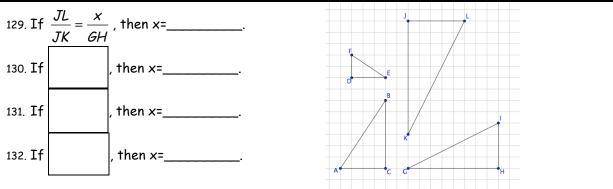
## Similar Triangles

Definition:				
<ul> <li>Similar Triangles</li> <li>Triangles are similar if they are either reductions or enlargements of one another.</li> </ul>				
<ul> <li>Triangles are similar if all corresponding angles are equal.</li> </ul>		OR: Triangles are similar if corresponding pairs of side lengths are proportional.		
A B B	∠A=∠D ∠C=∠F ∠B=∠E	A 2.2 C 1.4 B F	$\frac{AC}{DF} = \frac{2.2}{4.4} = \frac{1}{2}$ $\frac{BC}{EF} = \frac{1.4}{2.8} = \frac{1}{2}$ $AB = 3 = 1$	
	E	4.4 2.8 0 6	$\frac{d}{DE} = \frac{d}{6} = \frac{d}{2}$	

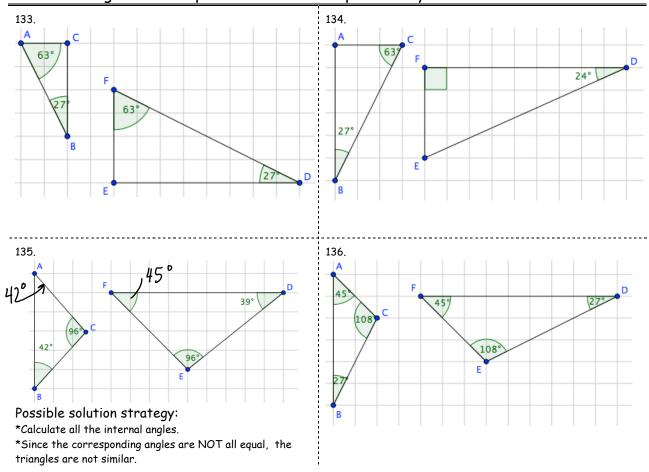
Challenge #7:





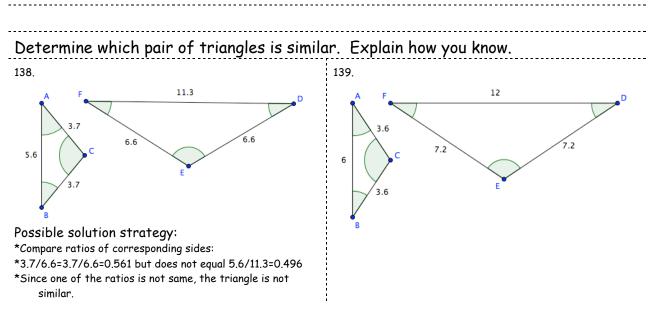


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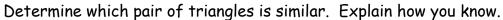


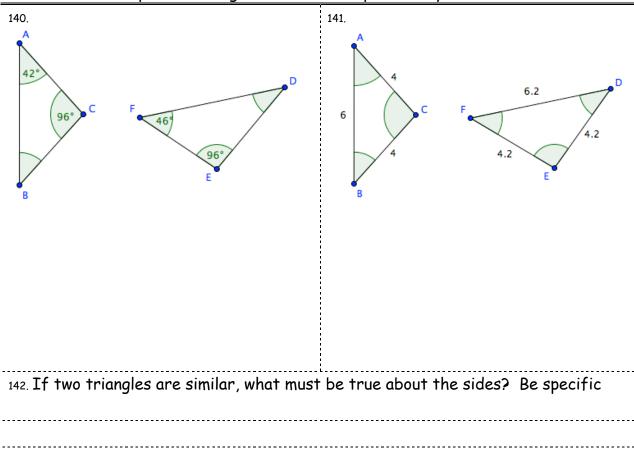
## Which triangles in each pair are similar? Explain how you know.

137. If two triangles are similar, what must be true about the angles? Be specific.

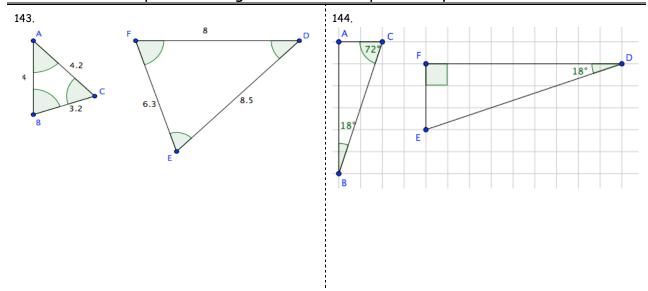


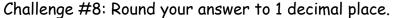
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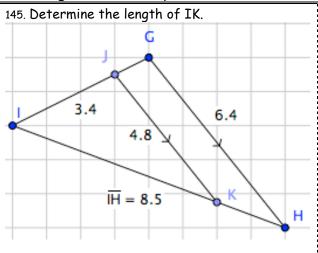




## Determine which pair of triangles is similar. Explain how you know.

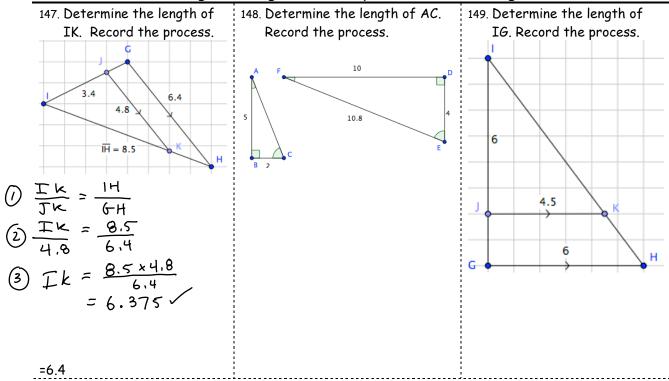




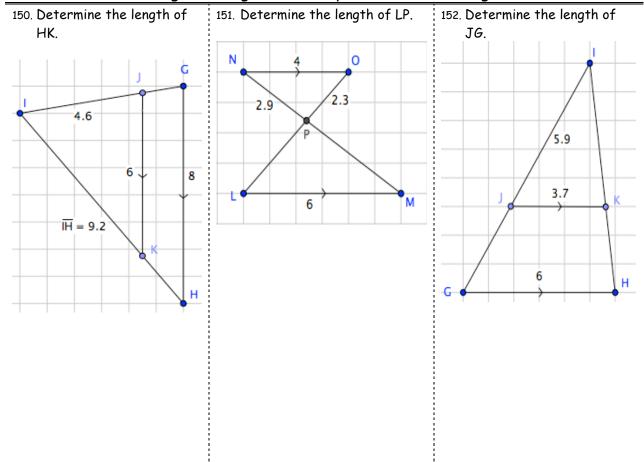


146. Rita is building a new roof on her home. She wants an A-frame roof that is in a ratio of 7 vertical feet to 12 horizontal feet. She knows the width of her home is 30feet wide. Determine how tall her roof is.

Determine the missing side lengths in each pair of similar triangles to 1 decimal.



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#### Determine the missing side lengths in each pair of similar triangles.

Using similar triangles to solve problems. Round your answer to the nearest tenth.

153. Rita is building a new roof on her home. She 154. Bella wants to estimate the height of her wants an A-frame roof that is in a ratio of 7 vertical feet to 12 horizontal feet. She knows the width of her home is 30 feet wide. Determine how tall her roof is.

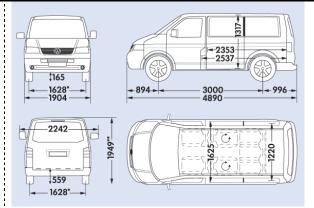
office building on a sunny day. She will use her shadow and the shadow of her office building to estimate the building's height. Bella is 1.4m tall and her shadow is 2m long. Determine the height of the building if the buildings shadow is 24m long.

#### Using similar triangles to solve problems.

- 155. Crazeen saw a water ski ramp at Lake Flyfar and determined the height of the ramp to be 1.66m and the ramp surface edge to be 6.4m. He wants to build a ramp on his home lake but wants to build a bigger one. He wants to keep the same proportions but knows the ramp surface edge can be no longer than 6.8m. Determine the height of his ramp to two decimals.
- 156. Jason found a photograph of a farmhouse with a roof that he really liked. The scale drawing said that the actual height of the roof was 4.5m tall and 6 meters to the center of the roof. He wants to have the same shape of roof for his new home. He has framed the lower part of the house and knows the distance to the center of the roof is 8m. Determine the height his roof.

#### Solve scale drawing problems. Round your answer to the nearest tenth.

157. Lumbarjay is going to cut down a large cedar tree on his property. He wants to make sure that it will not land on his house that is 24 meters from the base of the tree. He uses the sun's rays, his shadow and the shadow of the tree to help him make his decision. Lumbarjay is 1.8m tall and his shadow is 5m long. The shadow cast from the top of the tree is 32m long. Is his house in any danger? Explain how you know!



158. George is the kind of guy that would build a replica of a Chrysler Grand Voyager. If the total height of his model is 120mm how long will it be?

## Find real life scale drawings.

159. Search the newspaper, magazine or the internet for an example of a scale drawing that is an enlargement. Cut out the picture and:

- Determine the scale factor.
- Measure the object on the paper and included those measurements.
- Include the real life measurements

I. Real Life Enlargement:	II. Real life Reduction:
A. Object:	A. Object:
B. Source:	B. Source:
C. Paper measurements:	c. Paper measurements:
D. Actual measurements:	D. Actual measurements:
E. Scale factor:	E. Scale factor:
F. Was the scale factor ideal? Explain.	F. Was the scale factor ideal? Explain.